

**Amendments to the Claims:**

The following listing of claims will replace all prior versions, and listings, of claims in the application.

1. (Canceled) A method implemented in an apparatus for reconstructing a first signal  $(x(t))$ , the method comprising:
  - sampling a second signal  $(y(t))$  at a sub-Nyquist rate and at uniform intervals;
  - generating a set of sampled values  $(y_s[n], y(nT))$  from the second signal  $(y(t))$ ;
  - retrieving from said set of sampled values a set of shifts  $(t_n, t_k)$  and weights  $(c_n, c_{nr}, c_k)$ ;
  - and
  - reconstructing the first signal  $(x(t))$  based on the set of shifts  $(t_n, t_k)$  and weights  $(c_n, c_{nr}, c_k)$ .
2. (Canceled) Reconstruction method according to claim 1, wherein said set of regularly spaced sampled values comprises at least  $2K$  sampled values  $(y_s[n], y(nT))$ ,
  - wherein the class of said first signal  $(x(t))$  is known,
  - wherein the bandwidth  $(B, |\omega|)$  of said first signal  $(x(t))$  is higher than  $\omega_m = \pi/T$ ,  $T$  being the sampling interval,
  - wherein the rate of innovation  $(\rho)$  of said first signal  $(x(t))$  is finite,
  - wherein said first signal is faithfully reconstructed from said set of sampled values by solving a structured linear system depending on said known class of signal.

3. (Canceled) Reconstruction method according to claim 1, wherein the reconstructed signal  $x(t)$  is a faithful representation of the sampled signal  $y(t)$  or of a signal  $x_i(t)$  related to said sampled signal  $y(t)$  by a known transfer function  $\phi(t)$ .
4. (Canceled) Reconstruction method according to claim 3, wherein said transfer function  $\phi(t)$  includes the transfer function of a measuring device (7, 9) used for acquiring said second signal  $y(t)$  and/or of a transfer channel (5) over which said second signal  $y(t)$  has been transmitted.
5. (Canceled) Reconstruction method according to claim 1, wherein the reconstructed signal  $x(t)$  can be represented as a sequence of known functions  $\gamma(t)$  weighted by said weights  $(c_k)$  and shifted by said shifts  $(t_k)$ .
6. (Canceled) Reconstruction method according to claim 1, wherein the sampling rate is at least equal to the rate of innovation  $(\rho)$  of said first signal  $x(t)$ .
7. (Canceled) Reconstruction method according to claim 1, wherein a first system of equations is solved in order to retrieve said shifts  $(t_k)$  and a second system of equations is solved in order to retrieve said weights  $(c_k)$ .
8. (Canceled) Reconstruction method according to claim 7, wherein the Fourier coefficients  $(X[m])$  of said sample values  $(y_s[n])$  are computed in order to define the values in said first system of equations.

9. (Canceled) Reconstruction method according to claim 1, including the following steps:  
finding at least 2K spectral values ( $X[m]$ ) of said first signal ( $x(t)$ ),  
using an annihilating filter for retrieving said arbitrary shifts ( $t_n, t_k$ ) from said spectral values ( $X[m]$ ).
  
10. (Canceled) Reconstruction method according to claim 1, wherein said first signal ( $x(t)$ ) is a periodic signal with a finite rate of innovation ( $\rho$ ).
  
11. (Canceled) Reconstruction method according to claim 10, wherein said first signal ( $x(t)$ ) is a periodical piecewise polynomial signal, said reconstruction method including the following steps:  
finding 2K spectral values ( $X[m]$ ) of said first signal ( $x(t)$ ),  
using an annihilating filter for finding a differentiated version ( $x^{R+1}(t)$ ) of said first signal ( $x(t)$ ) from said spectral values,  
integrating said differentiated version to find said first signal.
  
12. (Canceled) Reconstruction method according to claim 10, wherein said first signal ( $x(t)$ ) is a finite stream of weighted Dirac pulses  $(x(t) = \sum_{k=0}^{K-1} c_k \delta(t - t_k))$ , said reconstruction method including the following steps:  
finding the roots of an interpolating filter to find the shifts ( $t_n, t_k$ ) of said pulses, solving a linear system to find the weights (amplitude coefficients) ( $c_n, c_k$ ) of said pulses.

13. (Canceled) Reconstruction method according to claim 1, wherein said first signal  $(x(t))$  is a finite length signal with a finite rate of innovation  $(\rho)$ .
14. (Canceled) Reconstruction method according to claim 13, wherein said reconstructed signal  $(x(t))$  is related to the sampled signal  $(y(t))$  by a sinc transfer function  $(\phi(t))$ .
15. (Canceled) Reconstruction method according to claim 13, wherein said reconstructed signal  $(x(t))$  is related to the sampled signal  $(y(t))$  by a Gaussian transfer function  $(\phi_{\sigma}(t))$ .
16. (Canceled) Reconstruction method according to claim 1, wherein said first signal  $(x(t))$  is an infinite length signal in which the rate of innovation  $(\rho, \rho_T)$  is locally finite, said reconstruction method comprising a plurality of successive steps of reconstruction of successive intervals of said first signal  $(x(t))$ .
17. (Canceled) Reconstruction method according to claim 16, wherein said reconstructed signal  $(x(t))$  is related to the sampled signal  $(y(t))$  by a spline transfer function  $(\phi(t))$ .
18. (Canceled) Reconstruction method according to claim 16, wherein said first signal  $(x(t))$  is a bilevel signal.
19. (Canceled) Reconstruction method according to claim 16, wherein said first signal  $(x(t))$  is a bilevel spline signal.

20. (Canceled) Reconstruction method according to claim 1, wherein said first signal  $x(t)$  is a CDMA or a Ultra-Wide Band signal.

21. Canceled.

22. (Previously Presented) A computer program product encoded with codes thereon executable by a digital processing system to:

sample a first signal  $y(t)$  at a sub-Nyquist rate and at uniform intervals;

generate a set of sampled values  $y_s[n]$ ,  $y(nT)$  from the first signal  $y(t)$ ;

retrieve from said set of sampled values a set of shifts  $(t_n, t_k)$  and weights  $(c_n, c_{nr}, c_k)$ ; and

reconstruct a second signal  $x(t)$  based on the set of shifts  $(t_n, t_k)$  and weights  $(c_n, c_{nr}, c_k)$ .

23. (Canceled) A method implemented in an apparatus for sampling a first signal  $x(t)$ , wherein said first signal  $x(t)$  can be represented over a finite time interval  $(\tau)$  by the superposition of a finite number  $(K)$  of known functions  $(\delta(t), \gamma(t), \gamma_r(t))$  delayed by arbitrary shifts  $(t_n, t_k)$  and weighted by arbitrary amplitude coefficients  $(c_n, c_k)$ , said method comprising:

convoluting said first signal  $x(t)$  with a sampling kernel  $((\phi(t), \phi(t))$  and using a regular sampling frequency  $(f, 1/T)$ ,

choosing said sampling kernel  $((\phi(t), \phi(t))$  and said sampling frequency  $(f, 1/T)$  such that sampled values  $(y_s[n], y(nT))$  completely specify said first signal  $x(t)$ , and

reconstructing said first signal  $x(t)$ ,

wherein said sampling frequency  $(f, 1/T)$  is lower than the frequency given by the Shannon theorem, but greater than or equal to twice said finite number  $(K)$  divided by said finite

time interval ( $\tau$ ).

24. (Canceled) Sampling method according to claim 23, wherein said first signal ( $x(t)$ ) is not bandlimited, and wherein said sampling kernel ( $\phi(t)$ ) is chosen so that the number of non-zero sampled values is greater than  $2K$ .

25. (Previously Presented) An apparatus for reconstructing a first signal ( $x(t)$ ) from a set of sampled values ( $y_s[n]$ ,  $y(nT)$ ), comprising:

a sampling device configured to generate the set of sampled values ( $y_s[n]$ ,  $y(nT)$ ) via sampling a second signal ( $y(t)$ ) at a sub-Nyquist rate and at uniform intervals; and

a reconstruction device configured to retrieve from said set of sampled values a set of shifts ( $t_n$ ,  $t_k$ ) and weights ( $c_n$ ,  $c_{nr}$ ,  $c_k$ ) with which said first signal ( $x(t)$ ) can be reconstructed.

26. (Previously Presented) The apparatus according to claim 25, wherein said set of regularly spaced sampled values comprises at least  $2K$  sampled values ( $y_s[n]$ ,  $y(nT)$ ),

wherein the class of said first signal ( $x(t)$ ) is known,

wherein the bandwidth ( $B$ ,  $|\omega|$ ) of said first signal ( $x(t)$ ) is higher than  $\omega_m = \pi/T$ ,  $T$  being the sampling interval,

wherein the rate of innovation ( $\rho$ ) of said first signal ( $x(t)$ ) is finite, and

wherein said first signal is faithfully reconstructed from said set of sampled values by solving a structured linear system depending on said known class of signal.

27. (Previously Presented) The apparatus according to claim 25, wherein the reconstructed

signal  $x(t)$  is a faithful representation of the sampled signal  $y(t)$  or of a signal  $x_i(t)$  related to said sampled signal  $y(t)$  by a known transfer function  $\phi(t)$ .

28. (Previously Presented) The apparatus according to claim 27, wherein said transfer function  $\phi(t)$  includes the transfer function of a measuring device (7, 9) used for acquiring said second signal  $y(t)$  and/or of a transfer channel (5) over which said second signal  $y(t)$  has been transmitted.

29. (Previously Presented) The apparatus according to claim 25, wherein the reconstructed signal  $x(t)$  can be represented as a sequence of known functions  $\gamma(t)$  weighted by said weights  $(c_k)$  and shifted by said shifts  $(t_k)$ .

30. (Previously Presented) The apparatus according to claim 25, wherein the sampling rate is at least equal to the rate of innovation  $(\rho)$  of said first signal  $x(t)$ .

31. (Previously Presented) The apparatus according to claim 25, wherein a first system of equations is solved in order to retrieve said shifts  $(t_k)$  and a second system of equations is solved in order to retrieve said weights  $(c_k)$ .

32. (Previously Presented) The apparatus according to claim 31, wherein the Fourier coefficients  $(X[m])$  of said sample values  $(y_s[n])$  are computed in order to define the values in said first system of equations.

33. (Previously Presented) The apparatus according to claim 25, further comprising:  
a filter configured to find at least 2K spectral values ( $X[m]$ ) of said first signal ( $x(t)$ ); and  
an annihilating filter configured to retrieve said arbitrary shifts ( $t_n, t_k$ ) from said spectral values ( $X[m]$ ).

34. (Previously Presented) The apparatus according to claim 25, wherein said first signal ( $x(t)$ ) is a periodic signal with a finite rate of innovation ( $\rho$ ).

35. (Previously Presented) The apparatus according to claim 34, wherein said first signal ( $x(t)$ ) is a periodical piecewise polynomial signal, the apparatus further comprising:  
a filter configured to find 2K spectral values ( $X[m]$ ) of said first signal ( $x(t)$ );  
an annihilating filter configured to find a differentiated version ( $x^{R+1}(t)$ ) of said first signal ( $x(t)$ ) from said spectral values; and  
an integrator configured to integrate said differentiated version to find said first signal.

36. (Previously Presented) The apparatus according to claim 34, wherein said first signal ( $x(t)$ ) is a finite stream of weighted Dirac pulses  $(x(t) = \sum_{k=0}^{K-1} c_k \delta(t - t_k))$ , the apparatus further comprising:

a filter configured to find the roots of an interpolating filter to find the shifts ( $t_n, t_k$ ) of said pulses, and solve a linear system to find the weights ( $c_n, c_k$ ) of said pulses.

37. (Previously Presented) The apparatus according to claim 25, wherein said first signal



$(x(t))$  is a finite length signal with a finite rate of innovation ( $\rho$ ).

38. (Previously Presented) The apparatus according to claim 37, wherein said reconstructed signal  $(x(t))$  is related to the sampled signal  $(y(t))$  by a sinc transfer function  $(\varphi(t))$ .

39. (Previously Presented) The apparatus according to claim 37, wherein said reconstructed signal  $(x(t))$  is related to the sampled signal  $(y(t))$  by a Gaussian transfer function  $(\varphi_{\sigma}(t))$ .

40. (Previously Presented) The apparatus according to claim 25, wherein said first signal  $(x(t))$  is an infinite length signal in which the rate of innovation ( $\rho, \rho_T$ ) is locally finite, wherein the reconstruction device is further configured to reconstruct successive intervals of said first signal  $(x(t))$ .

41. (Previously Presented) The apparatus according to claim 40, wherein said reconstructed signal  $(x(t))$  is related to the sampled signal  $(y(t))$  by a spline transfer function  $(\varphi(t))$ .

42. (Previously Presented) The apparatus according to claim 40, wherein said first signal  $(x(t))$  is a bilevel signal.

43. (Previously Presented) The apparatus according to claim 40, wherein said first signal  $(x(t))$  is a bilevel spline signal.

44. (Previously Presented) The apparatus according to claim 25, wherein said first signal  $(x(t))$  is a CDMA or a Ultra-Wide Band signal.

45. (Previously Presented) An apparatus for reconstructing a first signal  $(x(t))$  from a set of sampled values  $(y_s[n], y(nT))$ , comprising:

means for generating the set of sampled values  $(y_s[n], y(nT))$  by sampling a second signal  $(y(t))$  at a sub-Nyquist rate and at uniform intervals; and

means for retrieving from said set of sampled values a set of shifts  $(t_n, t_k)$  and weights  $(c_n, c_k)$  with which said first signal  $(x(t))$  can be reconstructed.

46. (Previously Presented) An apparatus for sampling a first signal  $(x(t))$ , wherein said first signal  $(x(t))$  can be represented over a finite time interval  $(\tau)$  by the superposition of a finite number  $(K)$  of known functions  $(\delta(t), \gamma(t), \gamma_r(t))$  delayed by arbitrary shifts  $(t_n, t_k)$  and weighted by arbitrary amplitude coefficients  $(c_n, c_k)$ , said method comprising:

a filter configured to convolute said first signal  $(x(t))$  with a sampling kernel  $((\varphi(t), \varphi(t))$  and using a regular sampling frequency  $(f, 1/T)$ ;

a sampling device configured to choose said sampling kernel  $((\varphi(t), \varphi(t))$  and said sampling frequency  $(f, 1/T)$  such that the sampled values  $(y_s[n], y(nT))$  completely specify said first signal  $(x(t))$ ; and

a reconstruction device configured to reconstruct said first signal  $(x(t))$ ,

wherein said sampling frequency  $(f, 1/T)$  is lower than the frequency given by the Shannon theorem, but greater than or equal to twice said finite number  $(K)$  divided by said finite time interval  $(\tau)$ .

47. (Previously Presented) The apparatus according to claim 46, wherein said first signal  $(x(t))$  is not bandlimited, and wherein said sampling kernel  $(\phi(t))$  is chosen so that the number of non-zero sampled values is greater than  $2K$ .

48. (Previously Presented) A computer program product encoded with codes thereon executable by a digital processing system to:

sample a first signal  $(x(t))$ , wherein said first signal  $(x(t))$  can be represented over a finite time interval  $(\tau)$  by the superposition of a finite number  $(K)$  of known functions  $(\delta(t), \gamma(t), \gamma_r(t))$  delayed by arbitrary shifts  $(t_n, t_k)$  and weighted by arbitrary amplitude coefficients  $(c_n, c_k)$ ;

convolute said first signal  $(x(t))$  with a sampling kernel  $((\phi(t), \phi(t))$  and using a regular sampling frequency  $(f, 1/T)$ ;

choose said sampling kernel  $((\phi(t), \phi(t))$  and said sampling frequency  $(f, 1/T)$  such that the sampled values  $(y_s[n], y(nT))$  completely specify said first signal  $(x(t))$ ; and

reconstruct said first signal  $(x(t))$ ,

wherein said sampling frequency  $(f, 1/T)$  is lower than the frequency given by the Shannon theorem, but greater than or equal to twice said finite number  $(K)$  divided by said finite time interval  $(\tau)$ .

49. (Previously Presented) An apparatus for sampling a first signal  $(x(t))$ , wherein said first signal  $(x(t))$  can be represented over a finite time interval  $(\tau)$  by the superposition of a finite number  $(K)$  of known functions  $(\delta(t), \gamma(t), \gamma_r(t))$  delayed by arbitrary shifts  $(t_n, t_k)$  and weighted by arbitrary amplitude coefficients  $(c_n, c_k)$ , said method comprising:

means for convoluting said first signal  $(x(t))$  with a sampling kernel  $((\phi(t), \phi(t))$  and using a regular sampling frequency  $(f, 1/T)$ ;

means for choosing said sampling kernel  $((\phi(t), \phi(t))$  and said sampling frequency  $(f, 1/T)$  such that the sampled values  $(y_s[n], y(nT))$  completely specify said first signal  $(x(t))$ ; and

means for reconstructing said first signal  $(x(t))$ ,

wherein said sampling frequency  $(f, 1/T)$  is lower than the frequency given by the Shannon theorem, but greater than or equal to twice said finite number  $(K)$  divided by said finite time interval  $(\tau)$ .